

<u>Funciones a derivar</u>	<u>Soluciones</u>
1) $y = x^2 + 3x - 2$	$y' = 2x + 3$
2) $y = -ax^2 + b$	$y' = -2ax$
3) $y = \frac{-x + 3}{2}$	$y' = -\frac{1}{2}$
4) $y = \frac{6x^8 - 3}{5}$	$y' = \frac{48x^7}{5}$
5) $y = mx + n$	$y' = m$
6) $y = (4 + 3x)x$	$y' = 4 + 6x$
7) $y = (3 + 2x)(3 - 2x)$	$y' = -8x$
8) $y = (ax^2 + bx + c)(ax - b)$	$y' = 3a^2x^2 - b^2 + ac$
9) $y = (-2x^2 + x - 1)\left(\frac{x-2}{2}\right)$	$y' = -3x^2 + 5x - \frac{3}{2}$
10) $y = (3x - 4)^4$	$y' = 12(3x - 4)^3$
11) $y = (2x^5 - 3)^6$	$y' = 60x^4(2x^5 - 3)^5$
12) $y = (2x - 3)^3(3x + 1)^2$	$y' = 6(2x - 3)^2(3x + 1)(5x - 2)$
13) $y = \frac{a}{x^n}$	$y' = -\frac{na}{x^{n+1}}$
14) $y = \frac{1}{x^4} + \frac{1}{x^3} + \frac{1}{x^2}$	$y' = -\frac{4}{x^5} - \frac{3}{x^4} - \frac{2}{x^3}$
15) $y = -\frac{2}{3}x^{-3}$	$y' = 2x^{-4}$
16) $y = \frac{a}{x^2} - \frac{b}{x} + c$	$y' = -\frac{2a}{x^3} + \frac{b}{x^2}$
17) $y = \frac{2x}{3x + 2}$	$y' = \frac{4}{(3x + 2)^2}$
18) $y = \frac{3x - 4}{x + 1}$	$y' = \frac{7}{(x + 1)^2}$
19) $y = \frac{3 - 4x}{5 + 2x}$	$y' = -\frac{26}{(2x + 5)^2}$
20) $y = \frac{ax + b}{cx + d}$	$y' = \frac{ad - bc}{(cx + d)^2}$
21) $y = \frac{x^2 + 1}{x + 1}$	$y' = \frac{x^2 + 2x - 1}{(x + 1)^2}$
22) $y = \frac{x + 2}{x^2 + x + 1}$	$y' = \frac{-x^2 - 4x - 1}{(x^2 + x + 1)^2}$
23) $y = \frac{1 - x^2}{2 + x^2}$	$y' = \frac{-6x}{(x^2 + 2)^2}$
24) $y = \frac{x}{x^2 - 1}$	$y' = -\frac{x^2 + 1}{(x^2 - 1)^2}$
25) $y = \frac{1}{a + x} + \frac{1}{a - x}$	$y' = \frac{1}{(x - a)^2} - \frac{1}{(x + a)^2}$

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26) $y = \frac{x^3 - 1}{x^3 + 1}$	$y' = \frac{6x^2}{(x^3 + 1)^2}$
27) $y = (2x + 3)^2$	$y' = 8x + 12$
28) $y = (4 - 5x)^3$	$y' = -15(4 - 5x)^2$
29) $y = \sqrt{2 - x}$	$y' = -\frac{1}{2\sqrt{2 - x}}$
30) $y = 3\sqrt{x^2 - 3}$	$y' = \frac{3x}{\sqrt{x^2 - 3}}$
31) $y = 2x\sqrt{5x}$	$y' = 3\sqrt{5x}$
32) $y = \frac{2}{\sqrt{1 + x}}$	$y' = -\frac{1}{\sqrt{(x + 1)^3}}$
33) $y = \sqrt[3]{4a + 7x}$	$y' = \frac{7}{3\sqrt[3]{(4a + 7x)^2}}$
34) $y = (x - \sqrt{1 - x^2})^2$	$y' = \frac{4x^2 - 2}{\sqrt{1 - x^2}}$
35) $y = x\sqrt{a + x}$	$y' = \frac{2a + 3x}{2\sqrt{a + x}}$
36) $y = (x + \sqrt{x})^2$	$y' = 2x + 1 + 3\sqrt{x}$
37) $y = 2\sqrt[5]{x^4 - 1}$	$y' = \frac{8x^3}{5\sqrt[5]{(x^4 - 1)^4}}$
38) $y = \ln\sqrt{\frac{x}{a}}$	$y' = \frac{1}{2x}$
39) $y = (1 - x)\ln(1 - x)$	$y' = -1 - \ln(1 - x)$
40) $y = \ln\frac{x + a}{x - a}$	$y' = \frac{1}{x + a} - \frac{1}{x - a}$
41) $y = \ln\left(1 + \frac{a}{x}\right)$	$y' = \frac{1}{x + a} - \frac{1}{x}$
42) $y = \ln\sqrt[3]{x^2}$	$y' = \frac{2}{3x}$
43) $y = \ln(x\sqrt{x + 1})$	$y' = \frac{1}{2x + 2} + \frac{1}{x}$
44) $y = \ln\sqrt[4]{1 - 2x^2}$	$y' = \frac{x}{2x^2 - 1}$
45) $y = \ln(2x + 3)^{1/2}$	$y' = \frac{1}{2x + 3}$
46) $y = \ln\frac{(x - 5)^3}{(x + 1)^2}$	$y' = \frac{3}{x - 5} - \frac{2}{x + 1}$
47) $y = \ln\sqrt[4]{\frac{(2x^2 - 3)^3}{x^2 - 5}}$	$y' = \frac{3x}{2x^2 - 3} - \frac{x}{2(x^2 - 5)}$

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48) $y = x^3 e^x + x^2 e^x$	$y' = e^x (x^3 + 4x^2 + 2x)$
49) $y = e^x + e^{-x}$	$y' = e^x - e^{-x}$
50) $y = e^{2 \operatorname{sen} x}$	$y' = 2e^{2 \operatorname{sen} x} \cos x$
51) $y = e^{3 \operatorname{sen} 4x}$	$y' = 12 e^{3 \operatorname{sen} 4x} \cos 4x$
52) $y = a^{\sqrt{x}}$	$y' = \frac{a^{\sqrt{x}} \ln a}{2\sqrt{x}}$
53) $y = \frac{2^x + 3^{-x}}{2}$	$y' = \frac{2^x \ln 2 - 3^{-x} \ln 3}{2}$
54) $y = x^3 e^{-3x}$	$y' = 3x^2 e^{-3x} (1 - x)$
55) $y = a^{nx}$	$y' = na^{nx} \ln a$
56) $y = 10^{\sqrt{x}}$	$y' = \frac{10^{\sqrt{x}} \ln 10}{2\sqrt{x}}$
57) $y = \ln \frac{e^x - 1}{e^x + 1}$	$y' = \frac{2e^x}{e^{2x} - 1}$
58) $y = \log_a (3x^2 + 5)$	$y' = \frac{6x}{3x^2 + 5} \cdot \frac{1}{\ln a}$
59) $y = \log \sqrt{\frac{1+x}{1-x}}$	$y' = \frac{1}{1-x^2} \cdot \frac{1}{\ln 10}$
60) $y = \ln \sqrt[3]{\frac{3x}{x+2}}$	$y' = \frac{2}{3x(x+2)}$
61) $y = \frac{\ln x}{\sqrt{x}}$	$y' = \frac{2 - \ln x}{2x\sqrt{x}} = \frac{\sqrt{x}(2 - \ln x)}{2x^2}$
62) $y = \ln \frac{x}{\sqrt{x^2 + a^2}}$	$y' = \frac{a^2}{x(x^2 + a^2)}$
63) $y = \ln \frac{(x-2)^3}{\sqrt{2x-1}}$	$y' = \frac{5x-1}{(x-2)(2x-1)}$
64) $y = \ln(x + \sqrt{x^2 - 1})$	$y' = \frac{1}{\sqrt{x^2 - 1}}$
65) $y = (3x+1)^{2x-3}$	$y' = (3x+1)^{2x-3} \cdot \left[ 2 \ln(3x+1) + \frac{3(2x-3)}{3x+1} \right]$
66) $y = x^{1/x}$	$y' = x^{1/x} \left( \frac{1 - \ln x}{x^2} \right)$
67) $y = \sqrt[3]{(x+1)^2}$	$y' = \sqrt[3]{(x+1)^2} \cdot \frac{2x - 2(x+1) \ln(x+1)}{x^2(x+1)}$
68) $y = 2x^{3x}$	$y' = 6x^{3x} (1 + \ln x)$
69) $y = 2x^{\cos x}$	$y' = 2x^{\cos x - 1} (\cos x - x \operatorname{sen} x \ln x)$
70) $y = x^a a^x e^x$	$y' = x^a a^x e^x \left( \frac{a}{x} + \ln a + 1 \right)$

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71) $y = \sqrt{x + \sqrt{x^2 - 1}}$	$y' = \frac{\sqrt{x + \sqrt{x^2 - 1}}}{2\sqrt{x^2 - 1}}$
72) $y = \frac{x+1}{x-1} + \frac{x}{\sqrt{x^2 - 1}}$	$y' = \frac{-2}{(x-1)^2} - \frac{1}{\sqrt{(x^2 - 1)^3}}$
73) $y = (2x+1)^3 \sqrt{x^2 - 1} + \frac{(2x+1)^3 x}{\sqrt{x^2 - 1}}$	$y' = 6(2x+1)^2 \sqrt{x^2 - 1} + \frac{(2x+1)^2 (8x^2 + x - 6)}{\sqrt{x^2 - 1}}$
74) $y = \operatorname{sen} 2x$	$y' = 2 \cos 2x$
75) $y = x \cos 2x$	$y' = \cos 2x - 2x \operatorname{sen} 2x$
76) $y = \operatorname{tg} \sqrt{x}$	$y' = \frac{1}{2\sqrt{x} \cos^2 \sqrt{x}} = \frac{1}{2\sqrt{x}} (1 + \operatorname{tg}^2 \sqrt{x})$
77) $y = \operatorname{sen}^3 3x$	$y' = 9 \operatorname{sen}^2 3x \cos 3x$
78) $y = 4 \cos^5 (2x - 1)$	$y' = -40 \cos^4 (2x - 1) \cdot \operatorname{sen} (2x - 1)$
79) $y = \operatorname{cotg} 4x^2$	$y' = -\frac{8x}{\operatorname{sen}^2 4x^2} = -8x(1 + \operatorname{cotg}^2 4x^2)$
80) $y = \frac{\operatorname{sen} x}{1 + \cos x}$	$y' = \frac{1}{1 + \cos x}$
81) $y = \frac{\cos x}{1 - \operatorname{sen} x}$	$y' = \frac{1}{1 - \operatorname{sen} x}$
82) $y = \operatorname{sen}^4 x - \cos^4 x$	$y' = 4 \operatorname{sen}^3 x \cos x + 4 \cos^3 x \operatorname{sen} x = 4 \operatorname{sen} x \cos x = 2 \operatorname{sen} 2x$
83) $y = \operatorname{arcsen} 2x$	$y' = \frac{2}{\sqrt{1 - 4x^2}}$
84) $y = \operatorname{arccos} \sqrt{x}$	$y' = \frac{-1}{2\sqrt{x - x^2}}$
85) $y = \operatorname{arctg}(x^2 + 1)$	$y' = \frac{2x}{x^4 + 2x^2 + 2}$
86) $y = \operatorname{arctg}(e^{-2x})$	$y' = \frac{-2e^{-2x}}{1 + e^{-4x}}$
87) $y = \operatorname{arctg}(\ln x)$	$y' = \frac{1}{x(1 + \ln^2 x)}$
88) $y = \frac{\operatorname{sen}^2 x - \cos x}{\operatorname{tg} x}$	$y' = \frac{2 \operatorname{sen}^2 x \cos^2 x + \operatorname{sen}^2 x \cos x - \operatorname{sen}^2 x + \cos x}{\operatorname{sen}^2 x}$
89) $y = \cos^2 3x^2$	$y' = -6x \operatorname{sen} 6x^2$